## CHAPTER - 1

## INTEGERS

- Integers are a bigger collection of numbers which is formed by whole numbers and their negatives.
- You have studied in the earlier class, about the representation of integers on the number line and their addition and subtraction.
- We now study the properties satisfied by addition and subtraction.
(a) Integers are closed for addition and subtraction both. That is, $a+b$ and $a-b$ are again integers, where $a$ and $b$ are any integers.
(b) Addition is commutative for integers, i.e., $a+b=b+a$ for all integers $a$ and $b$.
(c) Addition is associative for integers, i.e., $(\mathrm{a}+\mathrm{b})+\mathrm{c}=\mathrm{a}+(\mathrm{b}+\mathrm{c})$ for all integers $\mathrm{a}, \mathrm{b}$ and c .
(d) Integer 0 is the identity under addition. That is, $a+0=0+a=a$ for every integer $a$.
- We studied, how integers could be multiplied, and found that product of a positive and a negative integer is a negative integer, whereas the product of two negative integers is a positive integer. For example, $-2 \times 7=-14$ and $-3 \times-8=24$.
- Product of even number of negative integers is positive, whereas the product of odd number of negative integers is negative.
- Integers show some properties under multiplication.
(a) Integers are closed under multiplication. That is, $a \times b$ is an integer for any two integers a and $b$.
(b) Multiplication is commutative for integers. That is, $\mathrm{a} \times \mathrm{b}=\mathrm{b} \times \mathrm{a}$ for any integers a and b .
(c) The integer 1 is the identity under multiplication, i.e., $1 \times \mathrm{a}=\mathrm{a} \times 1=$ a for any integer a .
(d) Multiplication is associative for integers, i.e., $(a \times b) \times c=a \times(b \times c)$ for any three integers $\mathrm{a}, \mathrm{b}$ and c .
- Under addition and multiplication, integers show a property called distributive property. That is, $\mathrm{a} \times(\mathrm{b}+\mathrm{c})=\mathrm{a} \times \mathrm{b}+\mathrm{a} \times \mathrm{c}$ for any three integers $\mathrm{a}, \mathrm{b}$ and c .
- The properties of commutativity, associativity under addition and multiplication, and the distributive property help us to make our calculations easier.
- We also learnt how to divide integers. We found that,
(a) When a positive integer is divided by a negative integer, the quotient obtained is a negative integer and vice-versa.
(b) Division of a negative integer by another negative integer gives a positive integer as quotient.
- For any integer a, we have
(a) $a \div 0$ is not defined
( ) $\div 1=a$

