

CONCEPT MAP

Waves

Speed of transverse wave, $v = v\lambda$
 Speed of transverse wave on a stretched string,

$$v = \sqrt{\frac{T}{\mu}}$$

Transverse Wave : Individual particles of the medium execute simple harmonic motion about their mean position in a direction perpendicular to the direction of propagation of wave motion.

Wave Motion : It is a means of transferring energy and momentum from one point to another without any actual transportation of matter between these points.

Longitudinal Wave : Individual particles of the medium execute simple harmonic motion about their mean position along the same direction along which the wave is propagating.

Sound waves are longitudinal mechanical waves.

• Speed of sound wave in solids

$$v = \sqrt{\frac{Y}{\rho}}$$

• Speed of sound wave in fluid,

$$v = \sqrt{\frac{B}{\rho}}$$

• Speed of sound wave in gas,

$$v = \sqrt{\frac{\gamma P}{\rho}}$$

Principle of Superposition : When any number of waves meet simultaneously at a point in a medium, the net displacement at any given time is the algebraic sum of the displacement due to each wave at that time.

Standing Waves : When two sets of progressive wave trains of the same type traveling in same straight line in opposite direction superimpose, standing waves are formed.

Nodes : Points where amplitude of vibration is zero.

Antinodes : Points where amplitude of vibration is maximum.

Organ Pipe

Organ Pipe Closed at One End: Frequency of n^{th} normal mode of vibration,

$$v_n = (2n-1)v_1$$

 The frequency of fundamental mode is

$$v_1 = \frac{v}{4L_c}$$

Organ Pipe Open at Both Ends: Frequency of n^{th} normal mode of vibration

$$v_n = nv_1$$

The frequency of fundamental mode is

$$v_1 = \frac{v}{2L_o}$$

On String

Beats : The phenomenon of alternate variation in the intensity of sound with time at a particular position, when two sound waves of nearly same frequencies and amplitudes superimpose on each other.
 Beat frequency = number of beats per second = difference in frequency.

The wavelength of n^{th} mode of vibration of a stretched string is

$$\lambda_n = \frac{2L}{n}$$

and its frequency is

$$v_n = nv_1$$

The fundamental frequency of vibration of a stretched string

$$v_1 = \frac{1}{2L} \sqrt{\frac{T}{\mu}}$$

Doppler Effect : According to this effect, whenever there is a relative motion between a source of sound and listener, the apparent frequency of sound heard by the listener is different from the actual frequency of sound emitted by the source.

Apparent frequency,
$$v' = \frac{(v \pm v_o)v}{v \mp v_s}$$

where v is the actual frequency of sound emitted.

The upper sign on v_s (or v_o) is used when source (listener) moves towards the listener (source) while lower sign is used when it moves away.

Equation of plane progressive wave travelling with a velocity v along positive direction of x -axis

$$y = a \sin(kx - \omega t + \phi)$$

where $(kx - \omega t + \phi)$ is the phase.

Symbols Used

- a = amplitude of wave
- v_o = velocity of observer
- μ = linear mass density
- ρ = density
- L = length of the string
- v = velocity of sound
- Y = Young's modulus
- B = Bulk modulus
- v_1 = fundamental frequency
- γ = ratio of specific heats
- L_c = length of the closed pipe
- L_o = length of the open pipe
- v_s = velocity of source
- T = tension in the string
- P = pressure