

# CONCEPT MAP

## Kinematics

**Kinematics** : It is the branch of mechanics which deals with the study of motion of a body without taking into account the factors which cause motion.

**Uniform Circular Motion** : When a point object is moving on a circular path with a constant speed, then the motion of the object is said to be a uniform circular motion.

**Centripetal Acceleration** : The magnitude of centripetal acceleration is

$$a = \frac{v^2}{r} = r\omega^2$$

**Frame of Reference** : It is a system of coordinate axes attached to an observer having a clock with him, with respect to which the observer can describe position, displacement, acceleration etc of a moving object.

**Horizontal range** :

$$R = \frac{u^2 \sin 2\theta}{g}$$

**Projectile** : Any body given an initial velocity moves freely in space under the influence of gravity is called a projectile.

**Equation of Trajectory** :

$$y = \frac{g}{2u^2} x^2 \text{ (projected horizontally)}$$

$$y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta} \text{ (projected at an angle)}$$

**Maximum Height** :

$$H = \frac{u^2 \sin^2 \theta}{2g}$$

**Time of ascent = time of descent**

$$= \frac{u \sin \theta}{g}$$

**Time of flight**

$$T = \frac{2u \sin \theta}{g}$$

**Key Formulas**

- $v = \frac{d}{t}$
- $a = \frac{v-u}{t}$
- $v = u + at$
- $s = ut + \frac{1}{2} at^2$
- $v^2 - u^2 = 2as$
- $S_n = u + \frac{a}{2} (2n-1)$

- Distance** : It is the length of the actual path traversed by an object.
- Displacement** : It is defined as the shortest distance between the two positions of the body in a particular direction.

- Speed** =  $\frac{\text{distance travelled}}{\text{time taken}}$
- Velocity** =  $\frac{\text{displacement}}{\text{time taken}}$
- Average velocity** =  $\frac{\text{displacement}}{\text{time taken}}$
- Instantaneous velocity** =  $\lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$
- Acceleration** =  $\frac{\text{change in velocity}}{\text{time taken}}$
- Average acceleration** =  $\frac{\text{change in velocity}}{\text{time interval}}$
- Instantaneous acceleration** =  $\lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t} = \frac{dv}{dt} = \frac{d^2x}{dt^2}$

Velocity-time graph of a uniformly accelerated motion is a straight line inclined to time axis.

**Vector**

**Scalar**

Physical quantity having both magnitude and direction.

Physical quantity having only magnitude but no direction.

**Properties of Vector Product :**

$$\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$$

$$\vec{A} \times (\vec{B} + \vec{C}) = \vec{A} \times \vec{B} + \vec{A} \times \vec{C}$$

$$m(\vec{A} \times \vec{B}) = (m\vec{A}) \times \vec{B} = \vec{A} \times (m\vec{B}) = (\vec{A} \times \vec{B})m$$

**Properties of Scalar Product :**

- $\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}$
- $\vec{A} \cdot (\vec{B} + \vec{C}) = \vec{A} \cdot \vec{B} + \vec{A} \cdot \vec{C}$
- $m(\vec{A} \cdot \vec{B}) = (m\vec{A}) \cdot \vec{B} = \vec{A} \cdot (m\vec{B}) = (\vec{A} \cdot \vec{B})m$  where  $m$  is a scalar

Velocity-time graph of a uniform motion in one dimension is a straight line parallel to time axis. The area enclosed by this graph with time axis measures the displacement of an object in a given interval of time.

Position-time graph of a uniform motion in one dimension is a straight line inclined to time axis. The slope of the position-time graph with the axis tells the velocity of the object.

### Symbolic Used

- $u$  = initial velocity
- $v$  = final velocity
- $a$  = acceleration
- $t$  = time taken
- $s$  = displacement
- $S_n$  = displacement at  $n^{\text{th}}$  second
- $g$  = acceleration due to gravity
- $\omega$  = angular velocity