

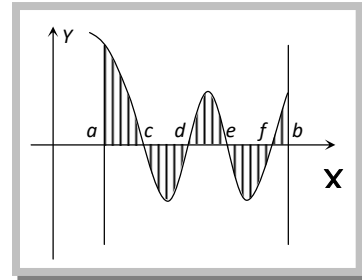
Sign convention for finding the Areas using Integration.

While applying the discussed sign convention, we will discuss the three cases.

Case I: In the expression $\int_a^b f(x) dx$ if $b > a$ and $f(x) > 0$ for all $a \leq x \leq b$, then this integration will give the area enclosed between the curve $f(x)$, x -axis and the line $x = a$ and $x = b$ which is positive. No need of any modification.

Case II: If in the expression $\int_a^b f(x) dx$ if $b > a$ and $f(x) < 0$ for all $a \leq x \leq b$, then this integration will calculate to be negative. But the numerical or the absolute value is to be taken to mean the area enclosed between the curve $y = f(x)$, x -axis and the lines $x = a$ and $x = b$.

Case III: If in the expression $\int_a^b f(x) dx$ where $b > a$ but $f(x)$ changes its sign a numbers of times in the interval $a \leq x \leq b$, then we must divide the region $[a, b]$ in such a way that we clearly get the points lying between $[a, b]$ where $f(x)$ changes its sign. For the region where $f(x) > 0$ we just integrate to get the area in that region and then add the absolute value of the integration calculated in the region where $f(x) < 0$ to get the desired area between the curve $y = f(x)$, x -axis and the line $x = a$ and $x = b$.



Hence, if $f(x)$ is as in above figure, the area enclosed by $y = f(x)$, x -axis and the lines $x = a$ and $x = b$ is given by

$$A = \int_a^c f(x) dx + \left| \int_c^d f(x) dx \right| + \int_d^e f(x) dx + \left| \int_e^f f(x) dx \right| + \int_f^b f(x) dx$$