

## Real and Imaginary Parts of a Complex Number.

If  $x$  and  $y$  are two real numbers, then a number of the form  $z = x + iy$  is called a complex number. Here ' $x$ ' is called the real part of  $z$  and ' $y$ ' is known as the imaginary part of  $z$ . The real part of  $z$  is denoted by  $\text{Re}(z)$  and the imaginary part by  $\text{Im}(z)$ .

If  $z = 3 - 4i$ , then  $\text{Re}(z) = 3$  and  $\text{Im}(z) = -4$ .

Note: A complex number  $z$  is purely real if its imaginary part is zero i.e.,  $\text{Im}(z) = 0$  and purely imaginary if its real part is zero i.e.,  $\text{Re}(z) = 0$ .

$i$  can be denoted by the ordered pair  $(0,1)$ .

The complex number  $(a, b)$  can also be split as  $(a, 0) + (0, 1)(b, 0)$ .

### Important Tips

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- ☞ A complex number is an imaginary number if and only if its imaginary part is non-zero. Here real part may or may not be zero.
- ☞ All purely imaginary numbers except zero are imaginary numbers but an imaginary number may or not be purely imaginary.
- ☞ A real number can be written as  $a + i \cdot 0$ , therefore every real number can be considered as a complex number whose imaginary part is zero. Thus the set of real number ( $\mathbb{R}$ ) is a proper subset of the complex number ( $\mathbb{C}$ ) i.e.,  $\mathbb{R} \subset \mathbb{C}$ .
- ☞ Complex number as an ordered pair : A complex number may also be defined as an ordered pair of real numbers and may be denoted by the symbol  $(a,b)$ . For a complex number to be uniquely specified, we need two real numbers in particular order.