

Number of Terms in the Expansion of $(a + b + c)^n$ and $(a + b + c + d)^n$.

$$\begin{aligned}(a + b + c)^n \text{ can be expanded as : } & (a + b + c)^n = \{(a + b) + c\}^n \\ & = (a + b)^n + {}^n C_1 (a + b)^{n-1} (c)^1 + {}^n C_2 (a + b)^{n-2} (c)^2 + \dots + {}^n C_n c^n \\ & = (n + 1)\text{term} + n \text{ term} + (n - 1)\text{term} + \dots + 1 \text{ term}\end{aligned}$$

$$\therefore \text{ Total number of terms} = (n + 1) + (n) + (n - 1) + \dots + 1 = \frac{(n + 1)(n + 2)}{2}.$$

$$\text{Similarly, Number of terms in the expansion of } (a + b + c + d)^n = \frac{(n + 1)(n + 2)(n + 3)}{6}.$$