

## Definition.

(1) Consider two equations,  $a_1x + b_1y = 0$  .....(i) and  $a_2x + b_2y = 0$  .....(ii)

Multiplying (i) by  $b_2$  and (ii) by  $b_1$  and subtracting, dividing by  $x$ , we get,  $a_1b_2 - a_2b_1 = 0$

The result  $a_1b_2 - a_2b_1$  is represented by  $\begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}$

Which is known as determinant of order two and  $a_1b_2 - a_2b_1$  is the expansion of this determinant. The horizontal lines are called rows and vertical lines are called columns.

Now let us consider three homogeneous linear equations

$$a_1x + b_1y + c_1z = 0, \quad a_2x + b_2y + c_2z = 0 \quad \text{and} \quad a_3x + b_3y + c_3z = 0$$

Eliminated  $x, y, z$  from above three equations we obtain

$$a_1(b_2c_3 - b_3c_2) - b_1(a_2c_3 - a_3c_2) + c_1(a_2b_3 - a_3b_2) = 0 \quad \text{.....(iii)}$$

The L.H.S. of (iii) is represented by  $\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$

It contains three rows and three columns, it is called a determinant of third order.

**Note:** The number of elements in a second order is  $2^2 = 4$  and the number of elements in a third order determinant is  $3^2 = 9$ .

(2) **Rows and columns of a determinant:** In a determinant horizontal lines counting from top  $1^{\text{st}}, 2^{\text{nd}}, 3^{\text{rd}}, \dots$  respectively known as rows and denoted by  $R_1, R_2, R_3, \dots$  and vertical lines counting left to right,  $1^{\text{st}}, 2^{\text{nd}}, 3^{\text{rd}}, \dots$  respectively known as columns and denoted by  $C_1, C_2, C_3, \dots$

(3) **Shape and constituents of a determinant:** Shape of every determinant is square. If a determinant of  $n$  order then it contains  $n$  rows and  $n$  columns.

i.e., Number of constituents in determinants =  $n^2$

(4) **Sign system for expansion of determinant:** Sign system for order 2, order 3, order 4, are

given by  $\begin{vmatrix} + & - \\ - & + \end{vmatrix}, \begin{vmatrix} + & - & + \\ - & + & - \\ + & - & + \end{vmatrix}, \begin{vmatrix} + & - & + & - \\ - & + & - & + \\ + & - & + & - \\ - & + & - & + \end{vmatrix}, \dots$

