## Equation of Ellipse in other form.

In the equation of the ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$, if $a>b$ or $a^{2}>b^{2}$ (denominator of $x^{2}$ is greater than that of $y^{2}$ ), then the major and minor axis lie along $x$-axis and $y$ axis respectively. But if $a<b$ or $a^{2}<b^{2}$ (denominator of $x^{2}$ is less than that of $y^{2}$ ), then the major axis of the ellipse lies along the $y$-axis and is of length $2 b$ and the minor axis along the $x$-axis and is of length $2 a$.
The coordinates of foci $S$ and $S^{\prime}$ are $(0, b e)$ and $(0,-b e)$ respectively.
The equation of the directrices $Z K$ and $Z^{\prime} K^{\prime}$ are $y= \pm b / e$ and eccentricity e is given by the formula $a^{2}=b^{2}\left(1-e^{2}\right)$ or $e=\sqrt{1-\frac{a^{2}}{b^{2}}}$


Difference between both ellipse will be clear from the following table.


## Basic fundamentals

|  | For $\mathbf{a}>\mathbf{b}$ | For b $>\mathbf{a}$ |
| :--- | :--- | :--- |
| Centre | $(0,0)$ | $(0,0)$ |
| Vertices | $( \pm a, 0)$ | $(0, \pm b)$ |
| Length of major axis | 2 a | 2 b |
| Length of minor axis | 2 b | 2 a |
| Foci | $( \pm a e, 0)$ | $(0, \pm b e)$ |
| Equation of directrices | $x= \pm a / e$ | $y= \pm b / e$ |
| Relation in a, b and e | $b^{2}=a^{2}\left(1-e^{2}\right)$ | $a^{2}=b^{2}\left(1-e^{2}\right)$ |
| Length of latus rectum | $\frac{2 b^{2}}{a}$ | $\frac{2 a^{2}}{b}$ |
| Ends of latus-rectum | $\left( \pm a e, \pm \frac{b^{2}}{a}\right)$ | $\left( \pm \frac{a^{2}}{b}, \pm b e\right)$ |
| Parametric equations | $(a \cos \phi, b \sin \phi)$ | $(a \cos \phi, b \sin \phi)(0 \leq \phi<2 \pi)$ |
| Focal radii | $S P=a-e x_{1}$ and $S^{\prime} P=a+e x_{1}$ | $S P=b-e y_{1}$ and $S^{\prime} P=b+e y_{1}$ |
| Sum of focal radii | 2 a | 2 b |
| $S P+S^{\prime} P=$ | 2 ae | 2 be |
| Distance between foci | $2 \mathrm{a} / \mathrm{e}$ | $2 \mathrm{~b} / \mathrm{e}$ |
| Distance between |  |  |


| directrices |  |  |
| :--- | :--- | :--- |
| Tangents at the vertices | $x=-a, x=a$ | $y=b, y=-b$ |

