## Equation of Pair of Tangents

If $P\left(x_{1}, y_{1}\right)$ be any point outside the hyperbola $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1$ then a pair of tangents $P Q, P R$ can be drawn to it from $P$.
The equation of pair of tangents $P Q$ and $P R$ is $S S_{1}=T^{2}$ where, $S=\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}-1, S_{1}=\frac{x_{1}^{2}}{a^{2}}-\frac{y_{1}^{2}}{b^{2}}-1, T=\frac{x x_{1}}{a^{2}}-\frac{y y_{1}}{b^{2}}-1$


Director circle: The director circle is the locus of points from which perpendicular tangents are drawn to the given hyperbola. The equation of the director circle of the hyperbola $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1$ is $x^{2}+y^{2}=a^{2}-b^{2}$


