## Equation of the Chord of contact of Tangents to a Parabola.

Let PQ and PR be tangents to the parabola $y^{2}=4 a x$ drawn from any external point $P\left(x_{1}, y_{1}\right)$ then QR is called the 'Chord of contact' of the parabola $y^{2}=4 a x$. The chord of contact of tangents drawn from a point $\left(x_{1}, y_{1}\right)$ to the parabola $y^{2}=4 a x$ is $y y_{1}=2 a\left(x+x_{1}\right)$
The equation is same as equation of the tangents at the point $\left(x_{1}, y_{1}\right)$.


Note: The chord of contact joining the point of contact of two perpendicular tangents always passes through focus.

If tangents are drawn from the point $\left(x_{1}, y_{1}\right)$ to the parabola $y^{2}=4 a x$, then the length of their chord of contact is $\frac{1}{|a|} \sqrt{\left(y_{1}^{2}-4 a x_{1}\right)\left(y_{1}^{2}+4 a^{2}\right)}$


The area of the triangle formed by the tangents drawn from $\left(x_{1}, y_{1}\right)$ to $y^{2}=4 a x$
and their chord of contact is $\frac{\left(y_{1}^{2}-4 a x_{1}\right)^{3 / 2}}{2 a}$.

