

1. Some Important Results on Number of Elements in Sets.

If A, B and C are finite sets and U be the finite universal set, then

$$(1) n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$(2) n(A \cup B) = n(A) + n(B) \Leftrightarrow A, B \text{ are disjoint non-void sets.}$$

$$(3) n(A - B) = n(A) - n(A \cap B) \text{ i.e. } n(A - B) + n(A \cap B) = n(A)$$

$$\begin{aligned} (4) n(A \Delta B) &= \text{Number of elements which belong to exactly one of A or B} \\ &= n((A - B) \cup (B - A)) \\ &= n(A - B) + n(B - A) \quad [\because (A - B) \text{ and } (B - A) \text{ are disjoint}] \\ &= n(A) - n(A \cap B) + n(B) - n(A \cap B) = n(A) + n(B) - 2n(A \cap B) \end{aligned}$$

$$(5) n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(A \cap C) + n(A \cap B \cap C)$$

$$(6) n(\text{Number of elements in exactly two of the sets A, B, C}) = n(A \cap B) + n(B \cap C) + n(C \cap A) - 3n(A \cap B \cap C)$$

$$(7) n(\text{Number of elements in exactly one of the sets A, B, C}) = n(A) + n(B) + n(C) - 2n(A \cap B) - 2n(B \cap C) - 2n(A \cap C) + 3n(A \cap B \cap C)$$

$$(8) n(A' \cup B') = n(A \cap B)' = n(U) - n(A \cap B)$$

$$(9) n(A' \cap B') = n(A \cup B)' = n(U) - n(A \cup B)$$