

Formulae for the Trigonometric Ratios of Sum and Differences of Two Angles.

$$(1) \sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$(2) \sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$(3) \cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$(4) \cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$(5) \tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$(6) \tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$(7) \cot(A + B) = \frac{\cot A \cot B - 1}{\cot A + \cot B}$$

$$(8) \cot(A - B) = \frac{\cot A \cot B + 1}{\cot B - \cot A}$$

$$(9) \sin(A + B) \cdot \sin(A - B) = \sin^2 A - \sin^2 B = \cos^2 B - \cos^2 A$$

$$(10) \cos(A + B) \cdot \cos(A - B) = \cos^2 A - \sin^2 B = \cos^2 B - \sin^2 A$$

$$(11) \tan A \pm \tan B = \frac{\sin A}{\cos A} \pm \frac{\sin B}{\cos B} = \frac{\sin A \cos B \pm \cos A \sin B}{\cos A \cos B} = \frac{\sin(A \pm B)}{\cos A \cdot \cos B}$$

$$\left(A \neq n\pi + \frac{\pi}{2}, B \neq m\pi \right)$$

$$(12) \cot A \pm \cot B = \frac{\sin(B \pm A)}{\sin A \cdot \sin B}$$

$$\left(A \neq n\pi, B \neq m\pi + \frac{\pi}{2} \right)$$