

Expansion of Hyperbolic Functions.

$$(1) \sinh x = \frac{e^x - e^{-x}}{2} = x + \frac{x^3}{3!} + \frac{x^5}{5!} + \frac{x^7}{7!} + \dots$$

$$(2) \cosh x = \frac{e^x + e^{-x}}{2} = 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \frac{x^6}{6!} + \dots$$

$$(3) \tanh x = \frac{e^x - e^{-x}}{e^x + e^{-x}} = x - \frac{x^3}{3} + 2x^5 - \frac{17}{315}x^7 + \dots$$

The expansion of $\coth x$, $\operatorname{cosech} x$ does not exist because $\coth(0) = \infty$, $\operatorname{cosech}(0) = \infty$.