

Gamma Function.

If m and n are non-negative integers, then
$$\int_0^{\pi/2} \sin^m x \cos^n x dx = \frac{\Gamma\left(\frac{m+1}{2}\right)\Gamma\left(\frac{n+1}{2}\right)}{2\Gamma\left(\frac{m+n+2}{2}\right)}$$

Where $\Gamma(n)$ is called gamma function which satisfied the following properties

$$\Gamma(n+1) = n\Gamma(n) = n! \quad \text{i.e.} \quad \Gamma(1) = 1 \text{ and } \Gamma(1/2) = \sqrt{\pi}$$

In place of gamma function, we can also use the following formula :

$$\int_0^{\pi/2} \sin^m x \cos^n x dx = \frac{(m-1)(m-3)\dots(2 \text{ or } 1)(n-1)(n-3)\dots(2 \text{ or } 1)}{(m+n)(m+n-2)\dots(2 \text{ or } 1)}$$

It is important to note that we multiply by $(\pi/2)$; when both m and n are even.