

1. Walli's Formula

$$\int_0^{\pi/2} \sin^n x dx = \int_0^{\pi/2} \cos^n x dx = \begin{cases} \frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \frac{n-5}{n-4} \cdots \frac{2}{3}, & \text{when } n \text{ is odd} \\ \frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \frac{n-5}{n-4} \cdots \frac{3}{4} \cdot \frac{1}{2} \cdot \frac{\pi}{2}, & \text{when } n \text{ is even} \end{cases}$$

$\int_0^{\pi/2} \sin^m x \cos^n x dx = \frac{(m-1)(m-3) \cdots (n-1)(n-3) \cdots}{(m+n)(m+n-2)} \quad [\text{If } m, n \text{ are both odd +ve integers or one odd +ve integer}]$

$$= \frac{(m-1)(m-3) \cdots (n-1)(n-3) \cdots}{(m+n)(m+n-2)} \cdot \frac{\pi}{2} \quad [\text{If } m, n \text{ are both +ve integers}]$$