

Leibnitz's Rule.

(1) If $f(x)$ is continuous and $u(x)$, $v(x)$ are differentiable functions in the interval $[a, b]$, then,

$$\frac{d}{dx} \int_{u(x)}^{v(x)} f(t) dt = f\{v(x)\} \frac{d}{dx} \{v(x)\} - f\{u(x)\} \frac{d}{dx} \{u(x)\}$$

(2) If the function $\phi(x)$ and $\psi(x)$ are defined on $[a, b]$ and differentiable at a point $x \in (a, b)$, and

$$\begin{aligned} f(x, t) \text{ is continuous, then, } & \frac{d}{dx} \left[\int_{\phi(x)}^{\psi(x)} f(x, t) dt \right] \\ &= \int_{\phi(x)}^{\psi(x)} \frac{d}{dx} f(x, t) dt + \left\{ \frac{d\psi(x)}{dx} \right\} f(x, \psi(x)) - \left\{ \frac{d\phi(x)}{dx} \right\} f(x, \phi(x)) \end{aligned}$$