Practical Applications of Elasticity.

- (i) The metallic parts of machinery are never subjected to a stress beyond elastic limit, otherwise they will get permanently deformed.
- (ii) The thickness of the metallic rope used in the crane in order to lift a given load is decided from the knowledge of elastic limit of the material of the rope and the factor of safety.
- (iii) The bridges are declared unsafe after long use because during its long use, a bridge under goes quick alternating strains continuously. It results in the loss of elastic strength.
- (iv) Maximum height of a mountain on earth can be estimated from the elastic behaviour of earth.

At the base of the mountain, the pressure is given by $P = h\rho g$ and it must be less than elastic limit (K) of earth's supporting material.

$$h < \frac{K}{\rho g} \qquad \qquad h_{\max} = \frac{K}{\rho g}$$
 K >P > hpg ... or

(v) In designing a beam for its use to support a load (in construction of roofs and bridges), it is advantageous to increase its depth rather than the breadth of the beam because the depression in rectangular beam.

$$\delta = \frac{Wl^3}{4Ybd^3}$$

To minimize the depression in the beam, it is designed as I-shaped girder.

- (vi) For a beam with circular cross-section depression is given by $\delta = \frac{WL^3}{12\pi r^4 Y}$
- (vii) A hollow shaft is stronger than a solid shaft made of same mass, length and material.

Torque required to produce a unit twist in a solid shaft $au_{\text{solid}} = \frac{\pi \eta r^4}{2l}$ (i)

and torque required to produce a unit twist in a hollow shaft $\tau_{\text{hollow}} = \frac{\pi \eta (r_2^4 - r_1^4)}{2l} \qquad(ii)$

From (i) and (ii),
$$\frac{\tau_{\text{hollow}}}{\tau_{\text{solid}}} = \frac{r_2^4 - r_1^4}{r^4} = \frac{(r_2^2 + r_1^2)(r_2^2 - r_1^2)}{r^4}$$
.....(iii)

Since two shafts are made from equal volume $\therefore \pi r^2 l = \pi (r_2^2 - r_1^2) l \Rightarrow r^2 = r_2^2 - r_1^2$

$$\frac{\tau_{\rm hollow}}{\tau_{\rm solid}} = \frac{r_2^2 + r_1^2}{r^2} > 1$$
 Substituting this value in equation (iii) we get,
$$\frac{\tau_{\rm hollow}}{\tau_{\rm solid}} = \frac{r_2^2 + r_1^2}{r^2} > 1$$

$$\therefore \tau \text{hollow} > \tau \text{solid}$$



i.e., the torque required to twist a hollow shaft is greater than the torque necessary to twist a solid shaft of the same mass, length and material through the same angle. Hence, a hollow shaft is stronger than a solid shaft.















