## Electric Potential Energy.

(1) Potential energy of a charge:Work done in bringing the given charge from infinity to a point in the electric field is known as potential energy of the charge. Potential can also be written as potential energy per unit charge. i.e. $\quad V=\frac{W}{Q}=\frac{U}{Q}$.
(2) Potential energy of a system of two charges:Since work done in bringing charge $Q_{2}$ from $\infty$ to point B is $W=Q_{2} V_{B}$, where $\mathrm{V}_{\mathrm{B}}$ is potential of point B due to charge $\mathrm{Q}_{1}$ i.e. $V_{B}=\frac{1}{4 \pi \varepsilon_{0}} \frac{Q_{1}}{r}$

$$
\text { So, } \quad W=U_{2}=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{Q_{1} Q_{2}}{r}
$$



This is the potential energy of charge $\mathrm{Q}_{2}$, similarly potential energy of charge $\mathrm{Q}_{1}$ will be $U_{1}=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{Q_{1} Q_{2}}{r}$
Hence potential energy of $\mathrm{Q}_{1}=$ Potential energy of $\mathrm{Q}_{2}=$ potential energy of system $U=k \frac{Q_{1} Q_{2}}{r}$ (in C.G.S. $\left.U=\frac{Q_{1} Q_{2}}{r}\right)$

Note: Electric potential energy is a scalar quantity so in the above formula take sign of $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$.
(3) Potential energy of a system of $\mathbf{n}$ charges:In a system of n charges electric potential energy is calculated for each pair and then all energies so obtained are added algebraically. i.e. $U=\frac{1}{4 \pi \varepsilon_{0}}\left[\frac{Q_{1} Q_{2}}{r_{12}}+\frac{Q_{2} Q_{3}}{r_{23}}+\ldots . . . ..\right]$ and in case of continuous distribution of charge. As $\Rightarrow U=\int V d Q$
E.g. Electric potential energy for a system of three charges


Potential energy $=\frac{1}{4 \pi \varepsilon_{0}}\left[\frac{Q_{1} Q_{2}}{r_{12}}+\frac{Q_{2} Q_{3}}{r_{23}}+\frac{Q_{3} Q_{1}}{r_{31}}\right]$

While potential energy of any of the charge say $\mathrm{Q}_{1}$ is $\frac{1}{4 \pi \varepsilon_{0}}\left[\frac{Q_{1} Q_{2}}{r_{12}}+\frac{Q_{3} Q_{1}}{r_{31}}\right]$
Note: For the expression of total potential energy of a system of n charges consider $\frac{n(n-1)}{2}$ number of pair of charges.
(4) Electron volt (eV):It is the smallest practical unit of energy used in atomic and nuclear physics. As electron volt is defined as "the energy acquired by a particle having one quantum of charge 1 e when accelerated by 1 volt" i.e. $1 \mathrm{eV}=1.6 \times 10^{-19} \mathrm{C} \times \frac{1 \mathrm{~J}}{\mathrm{C}}=1.6 \times 10^{-19} \mathrm{~J}=1.6 \times 10^{-12} \mathrm{erg}$ Energy acquired by a charged particle in eV when it is accelerated by V volt is $\mathrm{E}=($ charge in quanta) $\times$ (p.d. in volt)

## Commonly asked examples:

| S.No. | Charge | Accelerated by <br> p.d. | Gain in K.E. |
| :---: | :---: | :---: | :--- |
| (i) | Proton | $5 \times 10^{4} \mathrm{~V}$ | $\mathrm{~K}=\mathrm{e} \times 5 \times 10^{4} \mathrm{~V}=5 \times 10^{4} \mathrm{eV}=8 \times 10^{-15} \mathrm{~J}$ [JIPMER 1999] |
| (ii) | Electron | 100 V | $\mathrm{K}=\mathrm{e} \times 100 \mathrm{~V}=100 \mathrm{eV}=1.6 \times 10^{-17} \mathrm{~J}$ [MP PMT 2000; AFMC <br> $\mathbf{1 9 9 9}$ |
| (iii) | Proton | 1 V | $\mathrm{~K}=\mathrm{e} \times 1 \mathrm{~V}=1 \mathrm{eV}=1.6 \times 10^{-19} \mathrm{~J}$ [CBSE 1999] |
| (iv) | 0.5 C | 2000 V | $\mathrm{~K}=0.5 \times 2000=1000 \mathrm{~J}$ [JIPMER 2002] |
| (v) | $\alpha-$ |  |  |
| particle | $10^{6} \mathrm{~V}$ | $\mathrm{~K}=(2 \mathrm{e}) \times 10^{6} \mathrm{~V}=2 \mathrm{MeV}$ [MP PET/PMT 1998] |  |

(5) Electric potential energy of a uniformly charged sphere:Consider a uniformly charged sphere of radius $R$ having a total charge $Q$. The electric potential energy of this sphere is equal to the work done in bringing the charges from infinity to assemble the sphere.

$$
U=\frac{3 Q^{2}}{20 \pi \varepsilon_{0} R}
$$

## (6) Electric potential energy of a uniformly charged thin spherical shell:

$$
U=\frac{Q^{2}}{8 \pi \varepsilon_{0} R}
$$

(7) Energy density: The energy stored per unit volume around a point in an electric field is given by

$$
U_{e}=\frac{U}{\text { Volume }}=\frac{1}{2} \varepsilon_{0} E^{2} . \text { If in place of vacuum some medium is present then } U_{e}=\frac{1}{2} \varepsilon_{0} \varepsilon_{r} E^{2}
$$

## Concepts

(t) Electric potential energy is not localized but is distributed all over the field
© If a charge moves from one position to another position in an electric field so it's potential energy change and work done in this changing is $\boldsymbol{W}=\boldsymbol{U}_{\boldsymbol{f}}-\boldsymbol{U}_{\boldsymbol{i}}$
(s) If two similar charge comes closer potential energy of system increases while if two dissimilar charge comes closer potential energy of system decreases.

