

# Joule's Heating:

Whenever heat is converted into mechanical work or mechanical work is converted into heat, then the ratio of work done to heat produced always remains constant. i.e.

$$W \propto Q \text{ or } WQ = J$$

This is Joule's law and J is called mechanical equivalent of heat.

(1) From  $W = JQ$  if  $Q = 1$  then  $J = W$ . Hence the amount of work done necessary to produce unit amount of heat is defined as the mechanical equivalent of heat.

(2) J is neither a constant, nor a physical quantity rather it is a conversion factor which used to convert Joule or erg into calorie or kilo calories vice-versa.

(3) Value of

$$\begin{aligned} J &= 4.2 \text{ Joule/cal} = 4.2 \times 10^7 \text{ erg/cal} \\ &= 4.2 \times 10^3 \text{ Joule/kcal} \end{aligned}$$

(4) When water in a stream falls from height h, then its potential energy is converted into heat and temperature of water rises slightly.

From

$$W = JQ$$

$$\Rightarrow mgh = J (mc \Delta\theta)$$

[where m = Mass of water, c = Specific heat of water,

$\Delta\theta$  = temperature rise]

$$\Rightarrow \text{Rise in temperature } \Delta\theta = \frac{gh}{Jc} \text{ } ^\circ\text{C}$$

(5) The kinetic energy of a bullet fired from a gun gets converted into heat on striking the target. By this heat the temperature of bullet increases by  $\Delta\theta$ .

From  $W = JQ$

$$\Rightarrow \frac{1}{2}mv^2 = J(ms\Delta\theta)$$

[where m = Mass of the bullet, v = Velocity of the bullet, c = Specific heat of the bullet]

$\Rightarrow$  Rise in temperature,

$$\Delta t = \frac{v^2}{2Jc} \text{ } ^\circ\text{C}$$

If the temperature of bullet rises upto the melting point of the bullet and bullet melts then.

From

$$W = J(Q_{\text{Temperature change}} + Q_{\text{Phase change}})$$

$$\Rightarrow \frac{1}{2}mv^2 = J(mc\Delta\theta + mL)$$

; L = Latent heat of bullet

\(\Rightarrow\) Rise in temperature,

$$\Delta\theta = \frac{mv^2 - mL}{mc} \cdot C$$

(6) If m kg ice-block falls down through some height (h) and melts partially (m' kg) then its potential energy gets converted into heat of melting.

From  $W = JQ$

$$\Rightarrow mgh = Jm'L$$

$$\Rightarrow h = \frac{m'm}{JLg}$$

If ice-block melts completely then

$$m' = m \Rightarrow h = \frac{JLg}{m}$$