

Minimum Mass Hung From the String to Just Start the Motion.

(1) **When a mass m_1 placed on a rough horizontal plane:** Another mass m_2 hung from the string connected by pulley, the tension (T) produced in string will try to start the motion of mass m_1 .

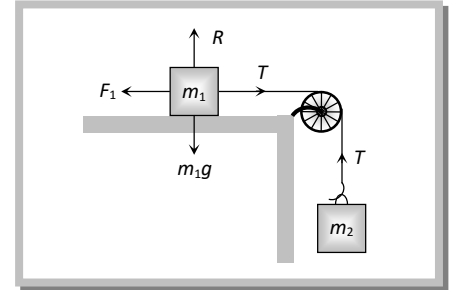
At limiting condition

$$T = F_l$$

$$\Rightarrow m_2 g = \mu R$$

$$\Rightarrow m_2 g = \mu m_1 g$$

$\therefore m_2 = \mu m_1$ This is the minimum value of m_2 to start the motion.



Note: In the above condition Coefficient of friction $\mu = \frac{m_2}{m_1}$

(2) **When a mass m_1 placed on a rough inclined plane:** Another mass m_2 hung from the string connected by pulley, the tension (T) produced in string will try to start the motion of mass m_1 .

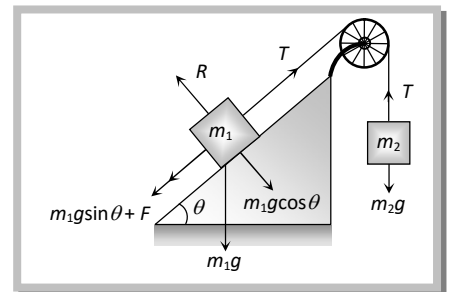
At limiting condition

$$\text{For } m_2 \quad T = m_2 g \quad \dots\dots (i)$$

$$\text{For } m_1 \quad T = m_1 g \sin \theta + F \Rightarrow T = m_1 g \sin \theta + \mu R$$

$$\Rightarrow T = m_1 g \sin \theta + \mu m_1 g \cos \theta \quad \dots\dots(ii)$$

From equation (i) and (ii) $m_2 = m_1 [\sin \theta + \mu \cos \theta]$
this is the minimum value of m_2 to start the motion



Note: In the above condition Coefficient of friction

$$\mu = \left[\frac{m_2}{m_1 \cos \theta} - \tan \theta \right]$$