

Angular Acceleration.

The rate of change of angular velocity is defined as angular acceleration.

If particle has angular velocity ω_1 at time t_1 and angular velocity ω_2 at time t_2 then,

$$\vec{\alpha} = \frac{\vec{\omega}_2 - \vec{\omega}_1}{t_2 - t_1}$$

Angular acceleration

(1) Instantaneous angular acceleration
$$\vec{\alpha} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{\omega}}{\Delta t} = \frac{d\vec{\omega}}{dt} = \frac{d^2 \vec{\theta}}{dt^2} .$$

(2) Unit: rad/sec^2

(3) Dimension: $[M^0 L^0 T^{-2}]$.

(4) If $\alpha = 0$, circular or rotational motion is said to be uniform.

(5) Average angular acceleration
$$\alpha_{av} = \frac{\omega_2 - \omega_1}{t_2 - t_1} .$$

(6) Relation between angular acceleration and linear acceleration
$$\vec{a} = \vec{\alpha} \times \vec{r} .$$

(7) It is an axial vector whose direction is along the change in direction of angular velocity i.e. normal to the rotational plane, outward or inward along the axis of rotation (depends upon the sense of rotation).