

## JEE-Main-26-07-2022-Shift-1 (Memory Based)

### Physics

**Question:** A charged particle is having acceleration  $\vec{a} = 2\hat{i} + 4\hat{j}$  while moving in an uniform magnetic field  $\vec{B} = \alpha\hat{i} - 3\hat{j}$ . Find  $\alpha$

**Options:**

- (a) 10
- (b) 2.5
- (c) 3
- (d) 4.5

**Answer:** (d)

**Solution:**

$$\therefore \vec{F} = q(\vec{v} \times \vec{B})$$

By property of cross product,

$$\vec{F} \perp \vec{B}$$

$$\vec{a} \perp \vec{B}$$

$$\therefore \vec{a} \cdot \vec{B} = 0$$

$$(2\hat{i} + 4\hat{j}) \cdot (\alpha\hat{i} - 3\hat{j}) = 0$$

**Question:** If in adiabatic process gas is compressed to  $\frac{1}{8}$  th of its volume, what will be the final pressure if Initial pressure is  $P_0$  (gas is monatomic)

**Options:**

- (a)  $12 P_0$
- (b)  $32 P_0$
- (c)  $42 P_0$
- (d)  $22 P_0$

**Answer:** (b)

**Solution:**

For monoatomic gas  $r = \frac{5}{3}$

In adiabatic process

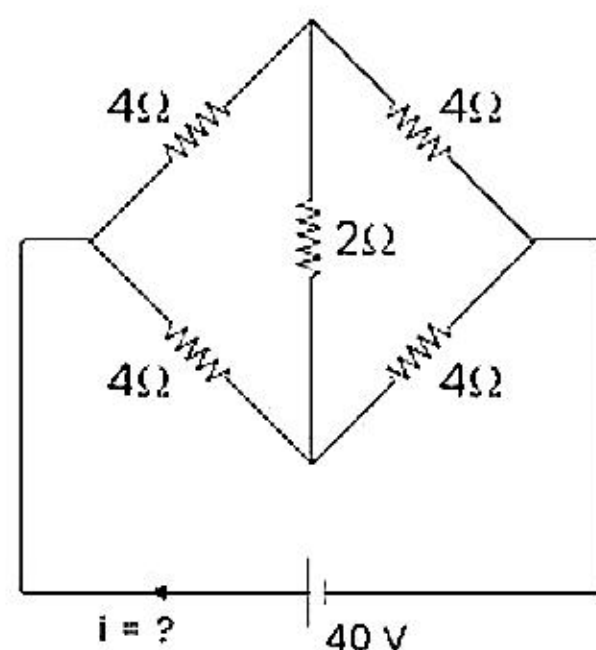
$$P_1 V_1^r = P_2 V_2^r$$

$$\therefore \frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^r = \left(\frac{V_0}{V_0/8}\right)^{5/3}$$

$$= (8)^{5/3} = 32$$

$$\therefore P_2 = 32P_1 = 32P_0$$

**Question:** What is the current through battery?



**Options:**

(a) 15 A

(b) 20 A

(c) 10 A

(d) 15 A

**Answer:** (c)

**Solution:**

Since it's a balanced Wheatstone bridge equivalent resistance becomes  $4\Omega$ . Since  $2\Omega$  resistance will not be considered.

$$\therefore i = \frac{40}{4} = 10A$$

**Question:** A monkey of 50 kg climbs a rope having maximum tension 350 N

Case A: Monkey climbs up with  $5 \text{ ms}^{-2}$

Case B: Monkey climbs down with  $4 \text{ ms}^{-2}$

In which case Rope will not break

**Options:**

(a) Case B: Break, Case A : break

(b) Case A: Not Break, Case B : break

(c) Case A: Break, Case B : Not break

(d) Case B: Not Break, Case A : Not break

**Answer:** (c)

**Solution:**

Breaking tension = 350 N

Case A  $T_A = m(g+a) = 50(10+5)$

= 750 N

Case B  $T_B = m(g-a) = 50(10-4)$

= 300 N

$\therefore$  Rope will break in case A

**Question:** A neutron and an electron of rest masses  $m_n$  and  $m_e$  are moving with speeds  $v$  and  $xv$  resp. If their de Broglie wavelength are equal then approximate value of  $x$  is consider  $m_e = 9.1 \times 10^{-31} \text{ kg}$  and  $m_n = 1.6 \times 10^{-27} \text{ kg}$ . Do not consider relativistic effect

**Options:**

- (a) 1600
- (b) 1758
- (c) 1880
- (d) 1990

**Answer:** (b)

**Solution:**

Using de Broglie eq.

$$\lambda = \frac{h}{mv}$$

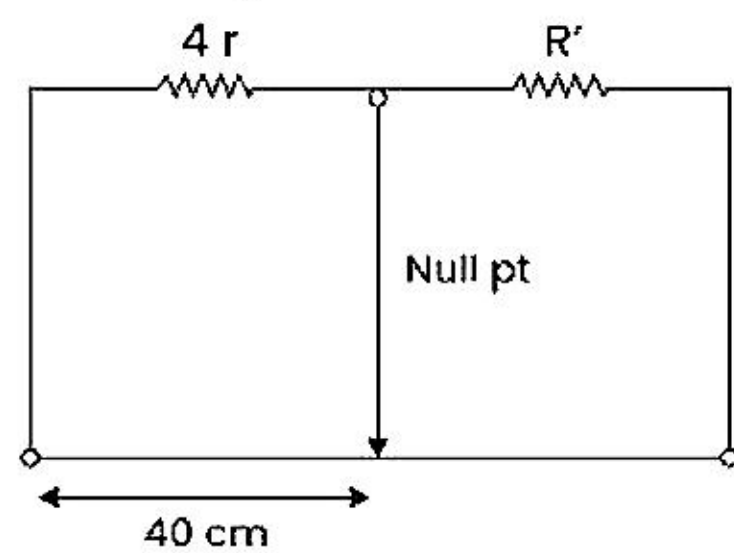
$$\therefore \lambda_e = \lambda_n$$

$$\frac{h}{m_e \times v} = \frac{h}{m_n v}$$

or

$$x = \frac{m_n}{m_e} = 1758$$

**Question:** A meter Bridge is as shown if a resistance of  $xr$  is connected in series with  $4r$ , new null point comes at 80 cm. Find  $x$ ?



**Options:**

- (a)  $x = 30$
- (b)  $x = 20$
- (c)  $x = 10$
- (d)  $x = 30$

**Answer:** (b)

**Solution:**

$$\frac{4r}{40} = \frac{R'}{60} \dots (1)$$

$$\& \frac{4r + xr}{80} = \frac{R'}{20} \dots (2)$$

Solving 1 and 2

$$\frac{4r + xr}{8r} = 3$$

$$\boxed{x = 20}$$

**Question:** If intensity of a wave is  $10 \text{ W m}^{-2}$  & it is passing through area of  $1 \text{ cm}^2$  & wavelength of wave is 900 nm. Find No. of photons passing per second.

**Options:**

- (a)  $6.51 \times 10^{10}$  photos / sec
- (b)  $8.51 \times 10^{16}$  photos / sec
- (c)  $3.51 \times 10^{16}$  photos / sec
- (d)  $4.51 \times 10^{16}$  photos / sec

**Answer:** (d)

**Solution:**

G. that

$$I = 100 \text{ w/m}^2$$

$$A = 1 \text{ cm}^2 = 1 \times 10^{-4} \text{ m}^2$$

$$\lambda = 900 \text{ nm} = 900 \times 10^{-9} \text{ m}$$

$$\text{No. of photos} = \frac{IAd}{GC}$$

$$= \frac{100 \times 1 \times 10^{-4} \times 900 \times 10^{-9}}{6.64 \times 10^{-34} \times 3 \times 10^2}$$

$$= 4.51 \times 10^{16} \text{ photos / sec}$$

**Question:** If in YDSE fringe width is 12 mm. What is new fringe width if whole setup is

immersed in water  $\mu = \frac{4}{3}$

**Options:**

- (a) 3 mm
- (b) 9 mm
- (c) 4 mm
- (d) 12 mm

**Answer:** (b)

**Solution:**

Given that  $\beta = 12 \text{ mm}$

Now set up is immersed in water  $\left( \mu = \frac{4}{3} \right)$

$$\beta' = \frac{\beta}{\mu}$$

$$\beta' = \frac{12}{4} \times 3$$

$$\boxed{\beta' = 9 \text{ mm}}$$

**Question:** Ratio of magnetic field at centre of two circular coils carrying same current and same radius with number of turns 200 and 400. Radius given was 20 cm for both

**Options:**

- (a)  $\frac{1}{2}$
- (b)  $\frac{2}{3}$

(c)  $\frac{3}{2}$

(d)  $\frac{5}{2}$

**Answer:** (a)

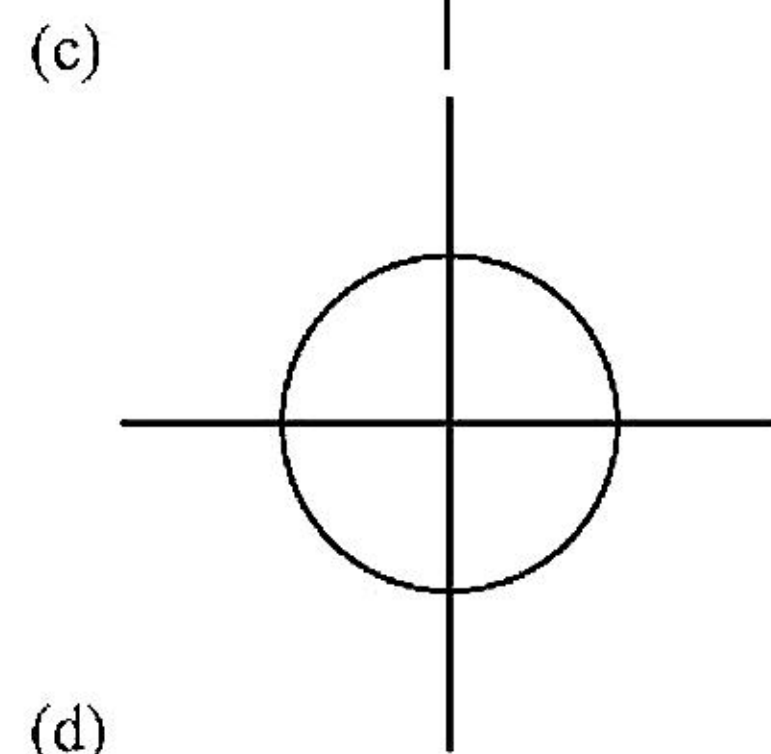
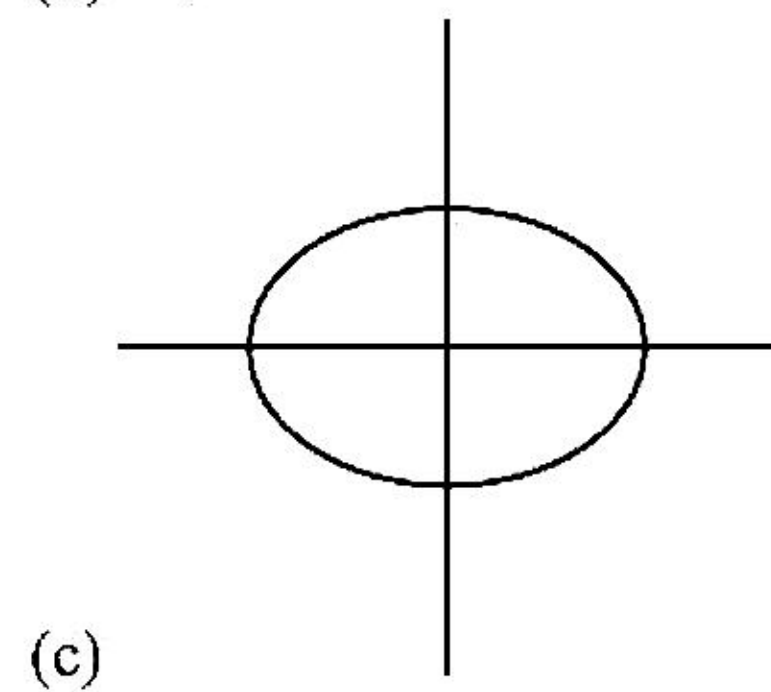
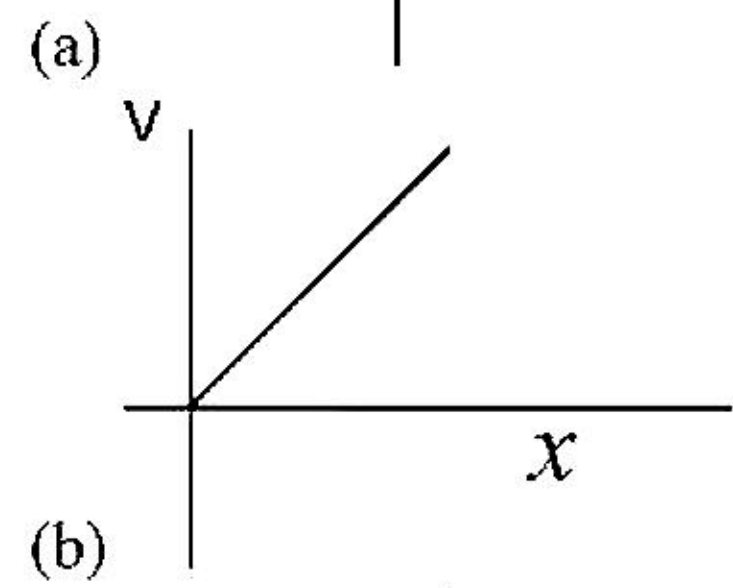
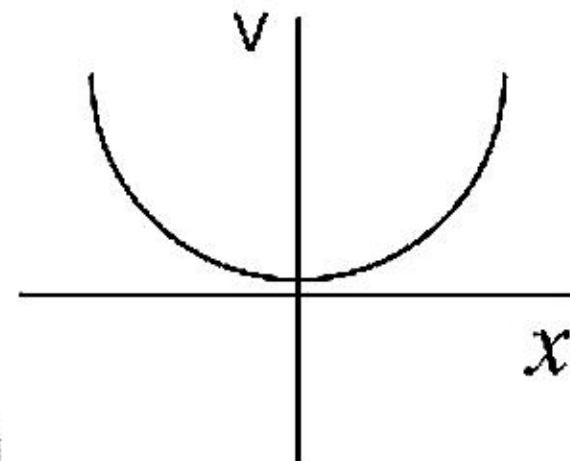
**Solution:**

$$B = N \frac{\mu_0 i}{2R}$$

$$\frac{B_1}{B_2} = \frac{N_1}{N_2} = \frac{200}{400} = \frac{1}{2}$$

**Question:** In linear SHM, variation of velocity of body against it's displacement is best represented by,

**Options:**



(d)

**Answer:** (c)

**Solution:**

$$v = \pm \omega \sqrt{A^2 - x^2}$$

$$v^2 = \omega^2 (A^2 - x^2)$$

$$v^2 = \omega^2 A^2 - \omega^2 x^2$$

$$v^2 + \omega^2 x^2 = \omega^2 A^2$$

$$\frac{v^2}{\omega^2 A^2} + \frac{\omega^2 x^2}{\omega^2 A^2} = 1$$

$$\frac{v^2}{(\omega A)^2} + \frac{x^2}{A^2} = 1 \quad (\text{ellipse})$$

**Question:** In LR circuit  $X_L = R$  and in LCR circuit  $X_L = X_C$ . Ratio of power factor in two situations is.

**Options:**

(a)  $\frac{1}{2}$

(b)  $\frac{1}{\sqrt{2}}$

(c)  $\sqrt{2}$

(d)  $\frac{2}{3}$

**Answer:** (b)

**Solution:**

Given that

For LR circuit

$$X_L = R$$

$$\cos \phi = \frac{R}{Z}$$

$$\cos \phi = \frac{R}{\sqrt{R^2 + R^2}}$$

$$(\cos \phi) = \frac{1}{\sqrt{2}} \dots (1)$$

$$X_L = X_C$$

$$\cos \phi = \frac{R}{Z}$$

$$(\cos \phi)_Z = \frac{R}{R} = 1 \dots (2)$$

From equation (1) and (2)

$$\frac{(\cos \phi)}{(\cos \phi)_Z} = \frac{1}{\sqrt{2}}$$

**Question:** Two projectiles at angles  $30^\circ$  and  $45^\circ$  reach their maximum heights in same time. Find the ratio of their initial velocities.

**Options:**

- (a) 1 : 1
- (b) 1 : 2
- (c) 2 : 1
- (d)  $\sqrt{2} : 1$

**Answer:** (d)

**Solution:**

$$\frac{2u_1 \sin 30^\circ}{g} = \frac{2u_2 \sin 45^\circ}{g}$$
$$\frac{u_1}{u_2} = \frac{\sin 45^\circ}{\sin 30^\circ} = \frac{\left(\frac{1}{\sqrt{2}}\right)}{\frac{1}{2}} = \sqrt{2} : 1$$

**Question:** If in EM wave  $B_0 = 2 \times 10^{-8} T$  find the amplitude of electric field

**Options:**

- (a)  $2NC^{-1}$
- (b)  $3NC^{-1}$
- (c)  $6NC^{-1}$
- (d)  $8NC^{-1}$

**Answer:** (c)

**Solution:**

Given that  $B_0 = 2 \times 10^{-8} T$

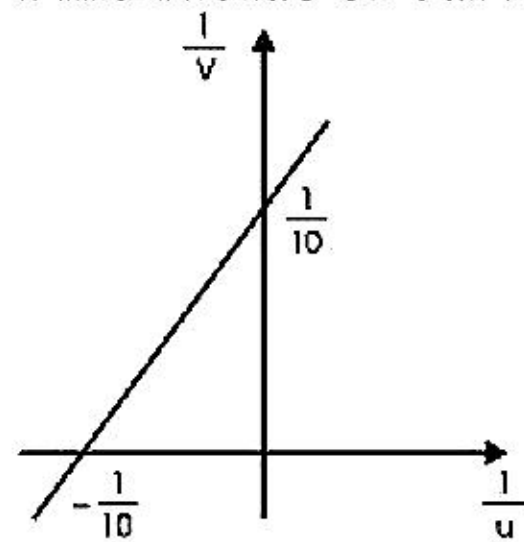
$$E_0 = ?$$

$$E_0 = B_0 C$$

$$E_0 = 2 \times 10^{-8} \times 3 \times 10^8$$

$$E_0 = 6 N / C$$

**Question:** For an equiconvex lens made of refractive index 1.5, following graph is given. Find radius of curvature of lens.



**Options:**

- (a) 10 cm
- (b) 20 cm

(c) 15 cm

(d) 20 cm

**Answer:** (a)

**Solution:**

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\frac{1}{f} = y - x$$

From graph

$$\frac{1}{f} = 0 - \left(-\frac{1}{10}\right)$$

$$f = 10\text{cm}$$

$$\frac{1}{f} = (\mu_R - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\frac{1}{10} = (1.5 - 1) \left( \frac{1}{R} + \frac{1}{R} \right)$$

$$\frac{1}{10} = \frac{1}{2} \left( \frac{2}{R} \right)$$

$$\boxed{R = 10\text{cm}}$$

**Question:** Radio can tune into 6MHz. Find the corresponding wavelength band

**Options:**

(a) 20m

(b) 30m

(c) 50m

(d) 70m

**Answer:** (a)

**Solution:**

$$\text{We know } \lambda = \frac{c}{f}$$

$$\text{So, } \lambda = \frac{C}{f_1}$$

$$\lambda_1 = \frac{3 \times 10^8}{6 \times 10^6} = 50\text{m}$$

$$\text{And } \lambda_2 = \frac{c}{f_2}$$

$$= \frac{3 \times 10^8}{10 \times 10^6} = 30\text{m}$$

$$\text{So wavelength band} = \lambda_1 - \lambda_2$$

$$= 50 - 30 = 20\text{m}$$



**Question:** Find the work done in splitting water droplet of radius  $R = 1 \text{ cm}$  into 729 droplets.  
Surface tension  $T = 75 \text{ dyne / cm}^2$ .

**Options:**

- (a)  $7.536 \times 10^{-3} \text{ J}$
- (b)  $7.536 \times 10^2 \text{ J}$
- (c)  $7.536 \times 10^3 \text{ J}$
- (d)  $75.36 \times 10^{-3} \text{ J}$

**Answer:** (a)

**Solution:**

According to question  $\frac{4}{3} \pi R^3 = n \times \frac{4}{3} \pi r^3$

$$(1)^3 = 729(r)^3$$

$$(r)^3 = \frac{1}{729}$$

$$\boxed{r = \frac{1}{9} \text{ m}}$$

$W_D = \text{Surface tension} \times \text{change in area}$

$$W_D = 75 \times 10^{-5+4} \times 4\pi$$

$$\left( 729 \times \left( \frac{1}{9} \right)^2 - (1)^2 \right)$$

$$W_D = 7.536 \times 10^{-3} \text{ J}$$

**Question:** Four capacitors having capacity 1,2,3,4  $\mu\text{F}$  connected in parallel. If 20V battery is connected across the system then find the charge flown through the battery

**Options:**

- (a)  $50 \mu\text{C}$
- (b)  $100 \mu\text{C}$
- (c)  $150 \mu\text{C}$
- (d)  $200 \mu\text{C}$

**Answer:** (d)

**Solution:**

If 1,2,3,4  $\mu\text{F}$  capacitors are connected in parallel then

$$C_{eq} = 1 + 2 + 3 + 4 = 10 \mu\text{F}$$

Given:  $V = 20 \text{ volt}$

So charge flown from the battery

$$q = C_{eq} V$$

$$q = 10 \times 20 \mu\text{C}$$

$$q = 200 \mu C$$

**Question:** A mass of  $M$  is attached at Top of find disc of same mass  $M$  and radius  $R$ . If point mass is given gentle push. Find  $\omega$  of disc when mass reaches bottom.

**Options:**

(a)  $\sqrt{\frac{9g}{3R}}$

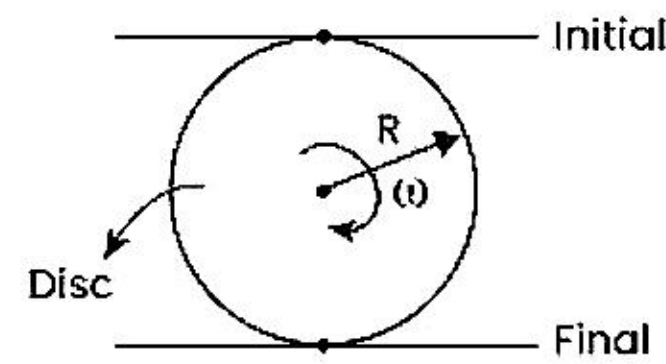
(b)  $\sqrt{\frac{8g}{3R}}$

(c)  $\sqrt{\frac{R}{3g}}$

(d)  $\sqrt{\frac{g}{R}}$

**Answer:** (b)

**Solution:**



$\omega$  = angular velocity at the instant.

When ball is at bottom.

As here is no friction as well as external force,

So, from conservation of mechanical energy

We have,  $\Delta k = -\Delta v$

Let us assume  $K_i$  (Initial kinetic energy = 0)

$$\therefore K_f - K_i = -(mg \times 2R)$$

$$\Rightarrow \frac{1}{2} I \omega^2 = mg \times 2R$$

$$\Rightarrow \frac{1}{2} \times \left( \frac{mR^2}{2} + mR^2 \right) \omega^2 = mg \times 2R$$

$$\Rightarrow \frac{3}{4} mR^2 \omega^2 = mg \times 2R$$

$$\Rightarrow \omega^2 = \frac{8g}{3R}$$

$$\Rightarrow \omega = \sqrt{\frac{8g}{3R}}$$